

Bit Operations

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Bit usage

- A bit can mean one of a pair of characteristics
- True or false
- Male or female
- Bit fields can represent larger classes
- There are 64 squares on a chess board, 6 bits could specify a position
- The exponent field of a float is bits 30-24 of a double word
- We could use a 4 bit field to store a color from black, red, green, blue, yellow, cyan, purple and white
- Should you store numbers from 0-15 in 4 bits or in a byte?

Bit operations

- Individual bits have values 0 and 1
- There are instructions to perform bit operations
- Using 1 as true and 0 as false
 - ▶ 1 and 1 = 1, or in C, `1 && 1 = 1`
 - ▶ 1 and 0 = 0, or in C, `1 && 0 = 0`
 - ▶ 1 or 0 = 1, or in C, `1 || 0 = 1`
- We are interested in operations on more bits
 - ▶ `10101000b & 11110000b = 10100000b`
 - ▶ `10101000b | 00001010b = 10101010b`
- These are called “bit-wise” operations
- We will not use bit operations on single bits, though we will test individual bits

Not operation

- C uses ! for a logical not
- C uses ~ for a bit-wise not

```
!0 == 1
```

```
!1 == 0
```

```
~0 == 1
```

```
~1 == 0
```

```
~10101010b == 01010101b
```

```
~0xff00 == 0x00ff
```

```
!1000000 == 0
```

Not instruction

- The `not` instruction flips all the bits of a number - one's complement
- `not` leaves the flags alone
- There is only a single operand which is source and destination
- For memory operands you must include a size prefix
- The sizes are `byte`, `word`, `dword` and `qword`
- The `C` operator is

```
not    rax        ; invert all bits of rax
not    dword [x]  ; invert double word at x
not    byte [x]   ; invert a byte at x
```

And operation

&	0	1
0	0	0
1	0	1

- C uses & for a logical and
- C uses && for a bit-wise and

11001100b & 00001111b == 00001100b

11001100b & 11110000b == 11000000b

0xabcdefab & 0xff == 0xab

0x0123456789abcdef & 0xff00ff00ff00ff00 == 0x010045008900cd00

- Bit-wise and is a bit selector

And instruction

- The `and` instruction performs a bit-wise and
- It has 2 operands, a destination and a source
- The source can be an immediate value, a memory location or a register
- The destination can be a register or memory
- Not both destination and source can be memory
- The sign flag and zero flag are set (or cleared)

```
mov    rax, 0x12345678
mov    rbx, rax
and    rbx, 0xf          ; rbx has the low nibble 0x8
mov    rdx, 0           ; prepare to divide
mov    rcx, 16          ; by 16
idiv   rcx              ; rax has 0x1234567
and    rax, 0xf         ; rax has the nibble 0x7
```


Or operation

	0	1
0	0	1
1	1	1

- C uses | for a logical and
- C uses || for a bit-wise and

11001100b | 00001111b == 11001111b

11001100b | 11110000b == 11111100b

0xabcdefab | 0xff == 0xabcdefff

0x0123456789abcdef | 0xff00ff00ff00ff00 == 0xff23ff67ffabffef

- Or is a bit setter

Or instruction

- The `or` instruction performs a bit-wise or
- It has 2 operands, a destination and a source
- The source can be an immediate value, a memory location or a register
- The destination can be a register or memory
- Not both destination and source can be memory
- The sign flag and zero flag are set (or cleared)

```
mov    rax, 0x1000
or     rax, 1           ; make the number odd
or     rax, 0xff00     ; set bits 15-8
```

Exclusive or operation

\sim		0	1
0		0	1
1		1	0

- C uses \sim for exclusive or

```
00010001b ^ 00000001b == 00010000b
```

```
01010101b ^ 11111111b == 10101010b
```

```
01110111b ^ 00001111b == 01111000b
```

```
0xaaaaaaaa ^ 0xffffffff == 0x55555555
```

```
0x12345678 ^ 0x12345678 == 0x00000000
```

- Exclusive or is a bit flipper

Exclusive or instruction

- The `xor` instruction performs a bit-wise exclusive or
- It has 2 operands, a destination and a source
- The source can be an immediate value, a memory location or a register
- The destination can be a register or memory
- Not both destination and source can be memory
- The sign flag and zero flag are set (or cleared)
- `mov rax, 0` uses 7 bytes
- `xor rax, rax` uses 3 bytes
- `xor eax, eax` uses 2 bytes

```
mov    rax, 0x1234567812345678
xor    eax, eax                ; set rax to 0
mov    rax, 0x1234
xor    rax, 0xf                ; change to 0x123b
```

Shift operations

- C uses `<<` for shift left and `>>` for shift right
- Shifting left introduces low order 0 bits
- Shifting right propagates the sign bit in C for signed integers
- Shifting right introduces 0 bits in C for unsigned integers
- Shifting left is like multiplying by a power of 2
- Shifting right is like dividing by a power of 2

```
101010b >> 3 == 10b
```

```
111111b << 2 == 11111100b
```

```
125 << 2 == 500
```

```
0xabcd >> 4 == 0xabc
```

Shift instructions

- Shift left: `shl`
- Shift right: `shr`
- Shift arithmetic left: `sarl`
- Shift arithmetic right: `sar`
- `shl` and `sarl` are the same
- `shr` introduces 0 bits on the top end
- `sar` propagates the sign bit
- There are 2 operands
 - ▶ A destination register or memory
 - ▶ In immediate number of bits to shift or `cl`
- The sign and zero flags are set (or cleared)
- The carry flag is set to the last bit shifted out

Extracting a bit field

- There are at least 2 ways to extract a bit field
- Shift right followed by an and
 - ▶ To extract bits $m - k$ with $m \geq k$, shift right k bits
 - ▶ And this value with a mask of $m - k + 1$ bits all set to 1
- Shift left and then right
 - ▶ Shift left until bit m is the highest bit
 - ▶ With 64 bit registers, shift left $63 - m$ bits
 - ▶ Shift right to get original bit k in position 0
 - ▶ With 64 bit registers, shift right $63 - (m - k)$ bits

Extracting a bit field with shift/and

Need to extract bits 9–3

1	1	0	0	0	1	1	1	1	0	0	1	0	1	1	0
15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0

Shift right 3 bits

0	0	0	1	1	0	0	0	1	1	1	1	0	0	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

And with 0x7f

0	0	0	0	0	0	0	0	0	1	1	1	0	0	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Extracting a bit field with shift/shift

Need to extract bits 9–3

1	1	0	0	0	1	1	1	1	0	0	1	0	1	1	0
15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0

Shift left 6 bits

1	1	1	0	0	1	0	1	1	0	0	0	0	0	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Shift right 9 bits

0	0	0	0	0	0	0	0	0	1	1	1	0	0	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Rotate instructions

- The `ror` instruction rotates the bits of a register or memory location to the right
- Values from the top end of the value start filling in the low order bits
- The `rol` instruction rotates left
- Values from the low end start filling in the top bits
- These are 2 operand instructions like the shift instructions
- The first operand is the value to rotate
- The second operand is the number of bits to rotate
- The second operand is either an immediate value or `cl`
- Assuming 16 bit rotates

```
1 ror 2 = 0100000000000000b
```

```
0xabcd rol 4 = 0xbcda
```

```
0x4321 ror 4 = 0x1342
```

Filling a field

- There are at least 2 ways of filling in a field
- You can shift the field and a mask and then use them
 - ▶ Working with a 64 bit register, filling bits $m - k$
 - ▶ Prepare a mask of $m - k + 1$ bits all 1
 - ▶ Shift the new value and the mask left k bits
 - ▶ Negate the mask
 - ▶ And the old value and the mask
 - ▶ Or in the new value for the field
- Use rotate and shift instructions and or in new value
 - ▶ Rotate the register right k bits
 - ▶ Shift the register right $m - k + 1$ bits
 - ▶ Rotate the register left $m - k + 1$ bits
 - ▶ Or in the new value
 - ▶ Rotate the register left k bits

Bit testing and setting

- It takes a few instructions to extract or set bit fields
- The same technique could be used to test or set single bits
- It can be more efficient to use special instructions operating on a single bit
- The `bt` instruction tests a bit
- `bts` tests a bit and sets it
- `btr` tests a bit and resets it (sets to 0)
- These are all 2 operand instructions
- The first operand is a register or memory location
- The second is the bit to work on, either an immediate value or a register

Set operations example code

- `rax` contains the bit number to work on
- This bit number could exceed 64
- We compute the quad-word of data which holds the bit
- We also compute the bit number within the quad-word

```
mov  rbx, rax           ; copy bit number to rbx
shr  rbx, 6             ; qword index of data to test
mov  rcx, rax           ; copy bit number to rcx
and  rcx, 0x3f          ; extract rightmost 6 bits
xor  edx, edx           ; set rdx to 0
bt   [data+8*rbx],rcx  ; test bit
setc dl                 ; edx equals the tested bit
bts  [data+8*rbx],rcx  ; set the bit, insert into set
btr  [data+8*rbx],rcx  ; clear the bit, remove
```